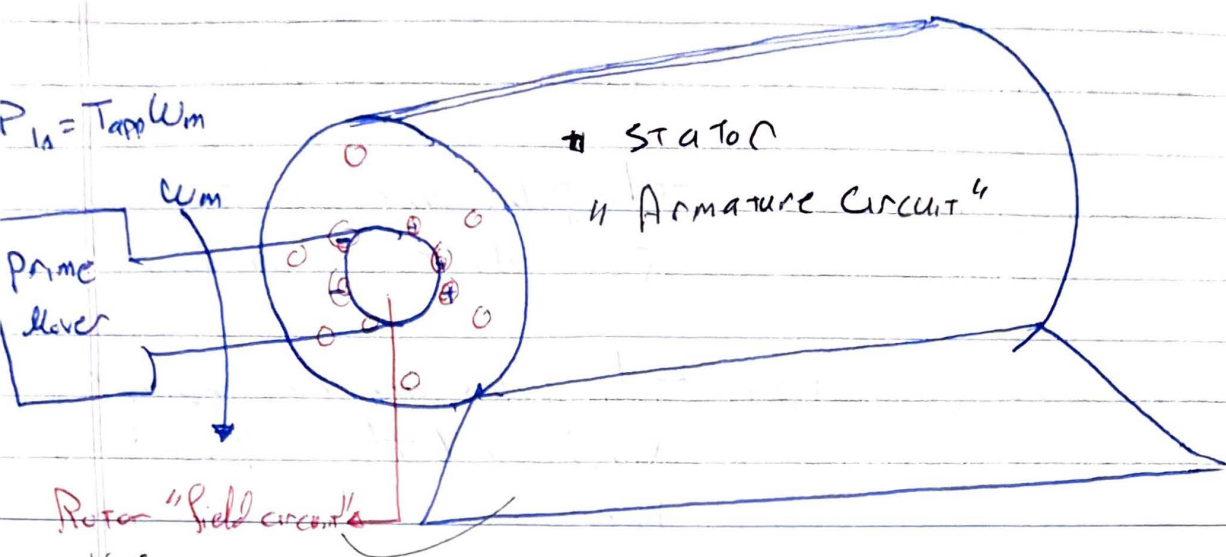


Synchronous Generator (SG)



flux

Prime mover: its the initial source of mechanical energy, it's any machine that converts fuel steam into a mechanical energy.

⊗ The synchronous generator has two main windings (flux is as 2nd)

1) Rotor or field winding where the machine flux is produced.

2) Stator or armature windings where the 3-φ voltage are induced (عند 3φ (جهد 3φ) (جهد 3φ))

⊗ operating principles

⊗ ~~A DC magnetic~~

⊗ A DC current is supplied to the rotor coil to produce a rotor magnetic field.

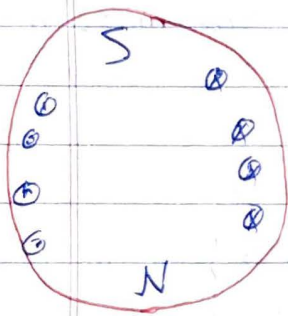
⊗ The Rotor rotates by means of external prime mover to produce a rotating magnetic field.

⊗ The rotating magnetic field will induce 3- ϕ Voltage across the stator (armature) winding.

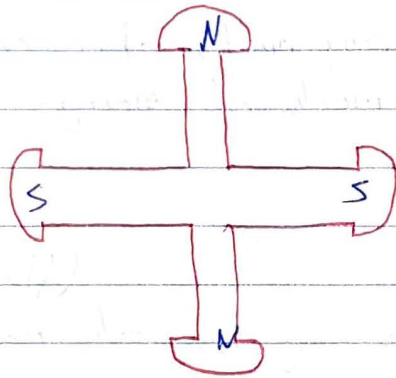
⊗ Types of Rotor in Synchronous generator:

① Salient pole rotor \Rightarrow The poles are sticking out from the rotor surface.

② Cylindrical Rotor type. The poles are constructed flush with the surface of the rotor.



$P=2$, Cylindrical type.

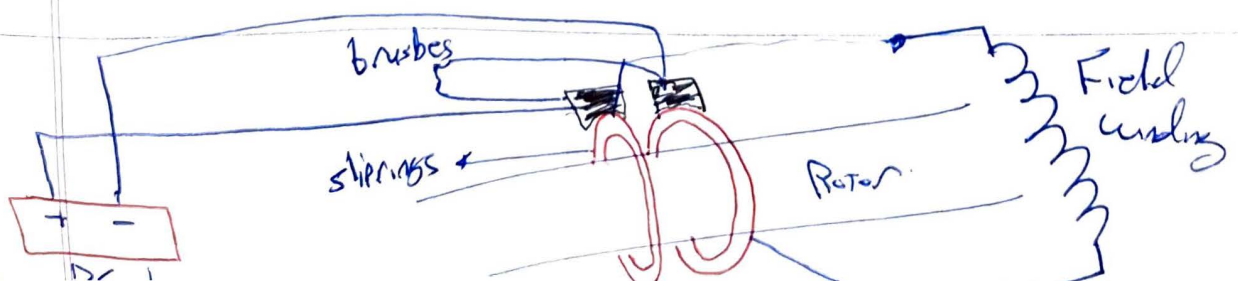


$P=4$
Salient-pole type

Note \therefore when $P > 4$ Salient pole machine is selected
when $P = 2, 4$ Cylindrical is usually used.

⊗ Methods to feed the Rotor or field circuit

① Sliprings & brushes \Rightarrow sliprings \Rightarrow Metal rings, encircling the shaft, but insulated.



Brushes go its a block of carbon compound that conducts electricity freely, but has very low friction.

This arrangement has two main problems :-

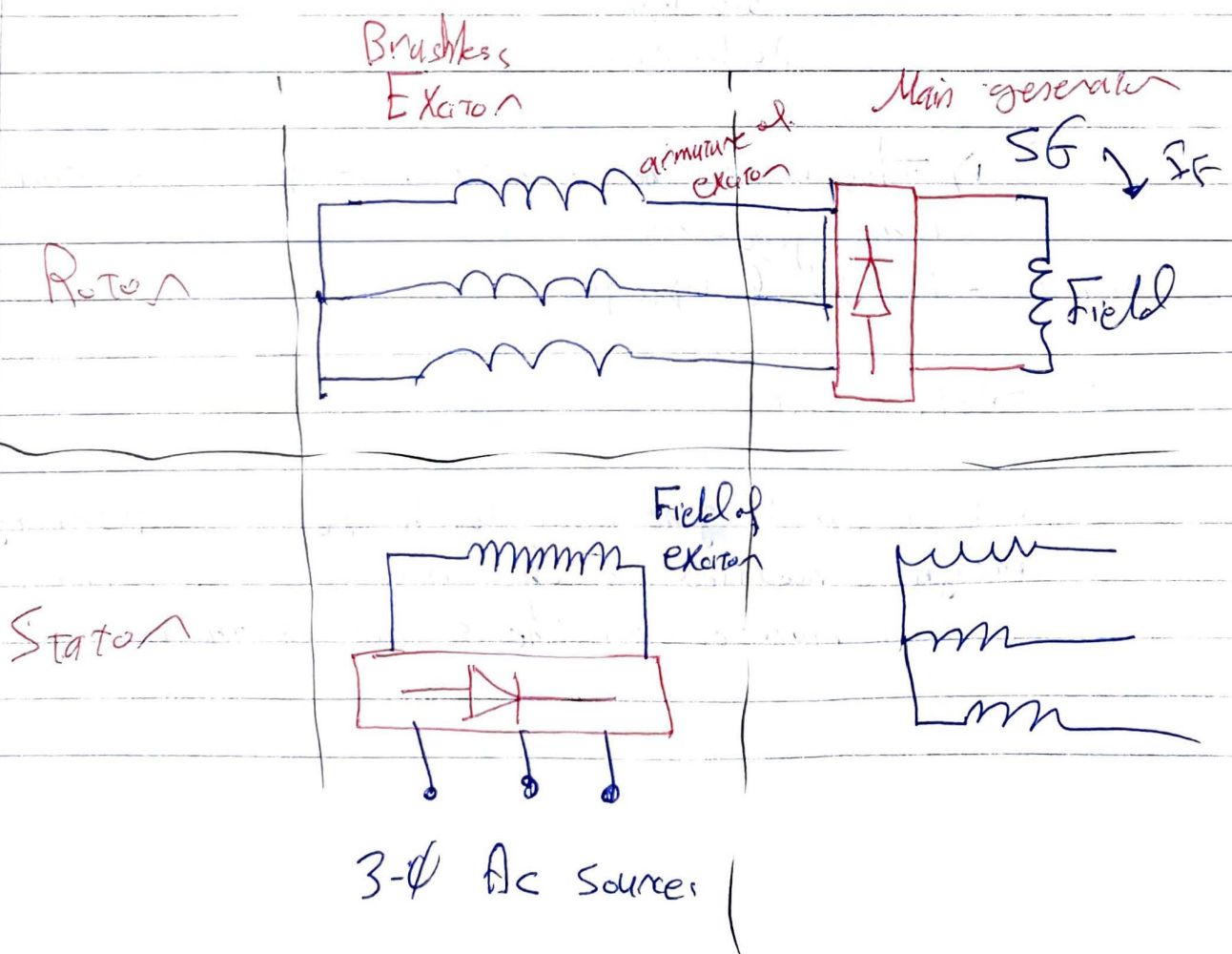
- 1) The brushes need regular maintenance.
- 2) The voltage drop across brushes may cause a power loss.

② Brushless exciter

③ Pilot excitor

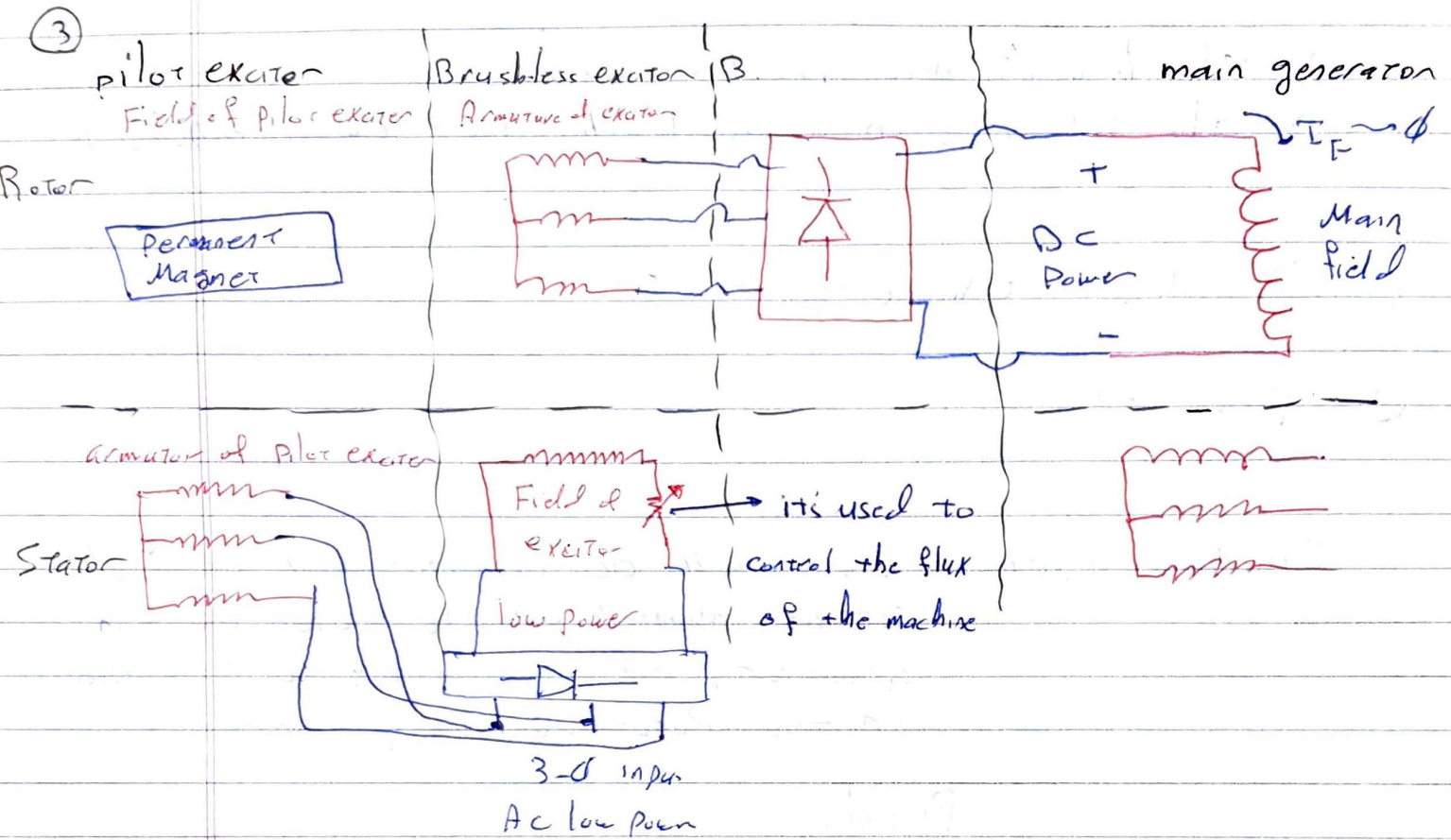
Brushless excitor go its a small ac generator with its field circuit mounted on the stator of main generator, and its armature windings, mounted on the rotor of main generator.

Don phase



② Brushless exciter

it's a small AC generator with its field mounted on the stator and its armature mounted on the rotor.



Disadvantages: ① This method needs a 3φ input power to run the main generator.

Advantages: - No Need input power

③ Pilot exciter

it's a small generator with ~~permanet~~ Permagneet magnet mounted on the rotor and its armature circuit mounted on the stator of the main generator.

The mechanical speed of SG

Synchronous \rightarrow The mechanical speed is synchronized with the electric frequency.

$$n_m = n_s = \frac{120 f_e}{p}$$

\downarrow Mechanical speed (Motor speed) \rightarrow Synchronous speed

where p is the number of poles,
 f_e is the electric frequency

$$n [\text{rpm}] = 60 F [\text{Hz}] \quad \text{rev/sec.}$$

$$n_m = \frac{2}{p} n_e \times \frac{60}{60} \quad \text{or} \quad \boxed{\omega_m = \frac{2}{p} \omega_e}$$

Internal or induced voltage of SG

The RMS value of L-N induced voltage, E_A , is given by

$$E_A = \frac{N_c \phi \omega_e}{\sqrt{2}} = \sqrt{2} \pi N_c \phi f_e$$

Armature \rightarrow

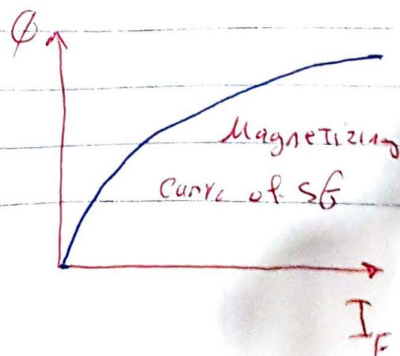
In general, the induced voltage is given by

$$E_A = K \phi \omega_e$$

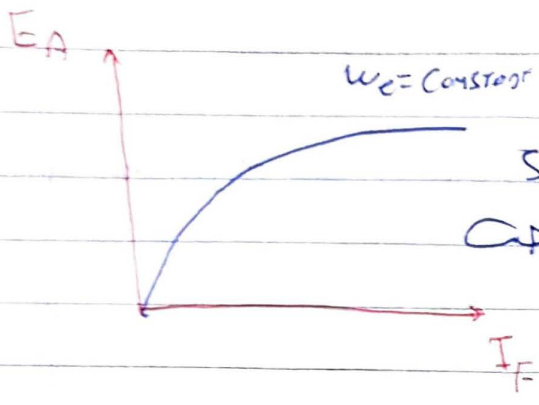
\rightarrow Flux of the machine
 \rightarrow Speed of machine
 \rightarrow Constant representing the construction of the machine

Note $\phi \propto I_F \Rightarrow \phi = C I_F$

\downarrow
Constant



It is also called back emf voltage



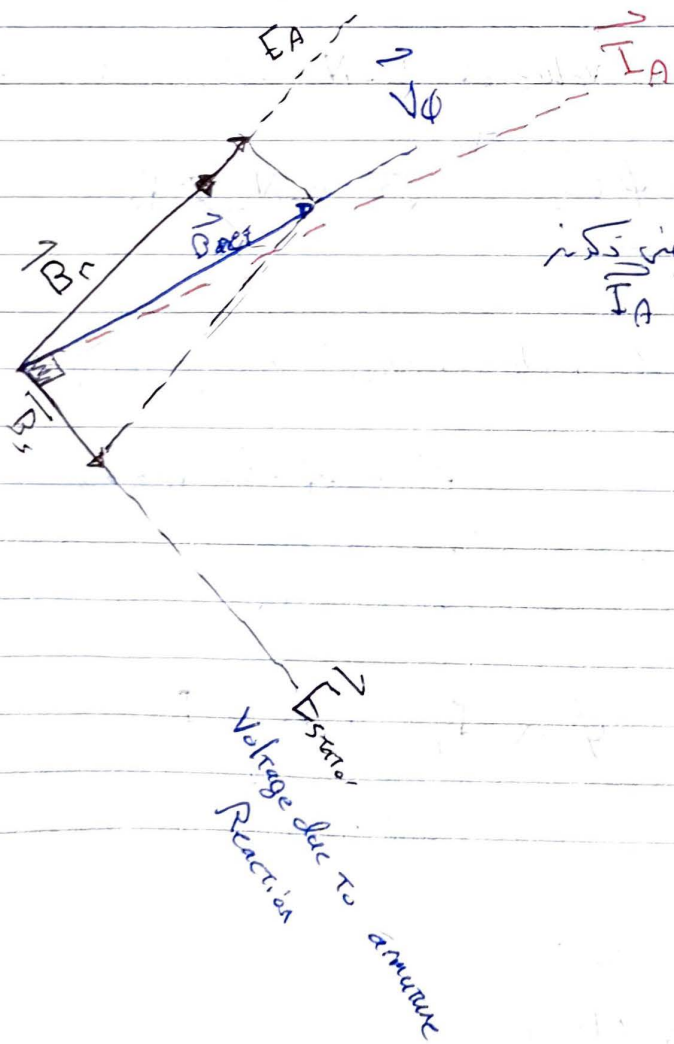
$$E_A = K\phi\omega_e = K\phi' = c' I_F$$

لأن ω_e ثابتة، فإن E_A تتناسب طردياً مع ϕ حتى الوصول إلى التشبع.
 $E_A = K\phi\omega$ العلاقة

Equivalent Circuit of SG

The terminal voltage, V_ϕ is different from the internal voltage, E_A of SG due to the armature reaction and the self impedance of the stator windings.

Armature Reaction → Distortion of air gap magnetic field due to the current flowing in the stator windings.



في حالة الحمل I_A يتغير B

E_{stator}
Voltage due to
Reaction

$$\vec{V}_\phi = \vec{E}_A + \vec{E}_{\text{STATOR}}$$

$$\vec{E}_{\text{STATOR}} = -jX I_A, \text{ where } X_0 \text{ is the reaction of armature reaction.}$$



$$\vec{V}_\phi = \vec{E}_A - jX I_A$$

we consider the self-impedance of the stator windings, the terminal phase voltage will be expressed as:

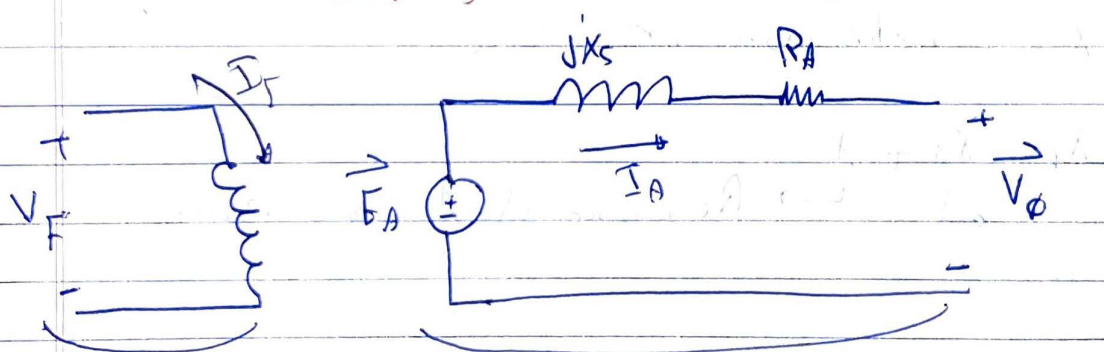
$$\vec{V}_\phi = \vec{E}_A - \underbrace{jX I_A}_{\text{self reactance}} - \underbrace{jX_A I_A}_{\text{self-reactance of stator winding}} - R_A I_A$$

$$\vec{V}_\phi = \vec{E}_A - j(X + X_A) I_A - R_A I_A$$

$$\vec{V}_\phi = \vec{E}_A - jX_s I_A - R_A I_A$$

where $X_s = X + X_A$

↳ synchronous reactance

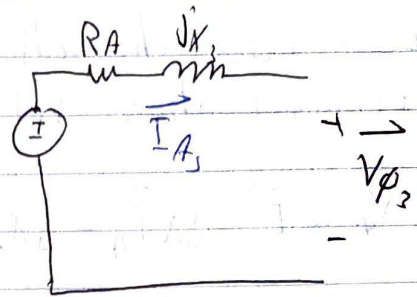
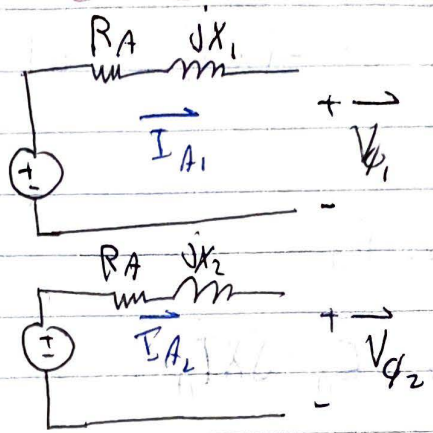
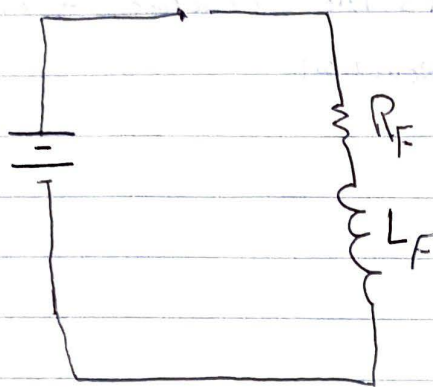


Field circuit

per-phase equivalent circuit

The full equivalent circuit of 3 ϕ SF

Dc supply
↓
 V_P



Field circuit
"Rotor"

Armature circuit
"Stator"

R_A : self-resistance of stator winding.
 X_s : synchronous reactance

$$X_1 = X_A + X$$

self-reactance of stator winding \leftarrow \leftarrow Reactance of Armature reaction

$$\left. \begin{matrix} B_m \\ B_s \end{matrix} \right\} \Rightarrow B_{net} \quad \swarrow \quad V_\phi$$

Y -connection

$$V_L = \sqrt{3} V_\phi$$

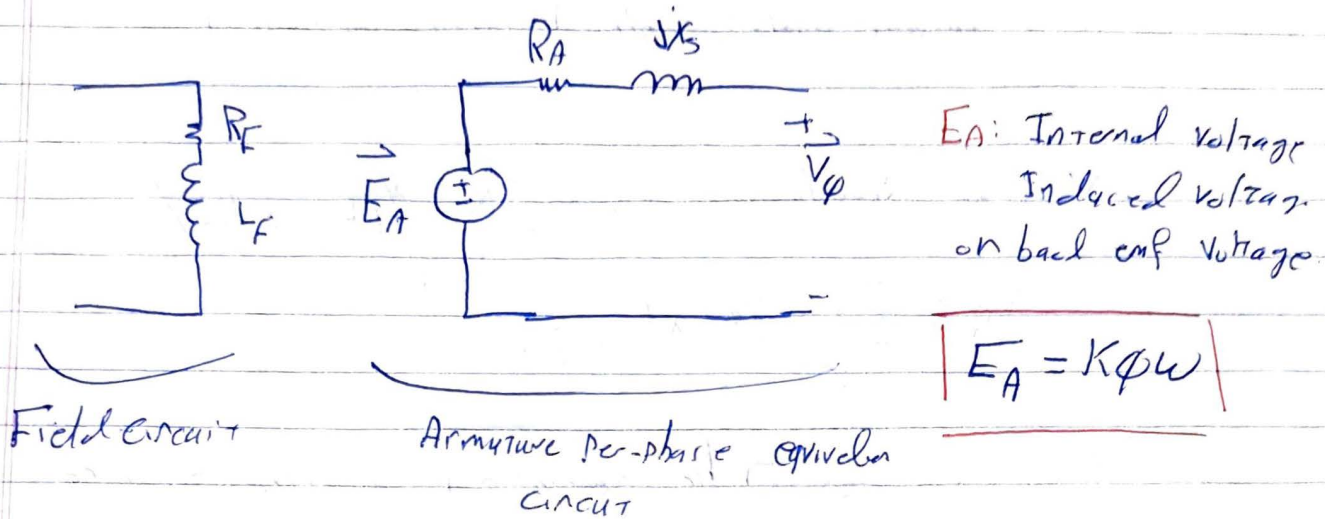
$$\vec{I}_L = \vec{I}_\phi + \vec{I}_A$$

Δ connection

$$V_L = V_\phi$$

$$I_L = \sqrt{3} I_\phi = \sqrt{3} I_A$$

The per phase equivalent circuit and machine KVL equation



Machine KVL equation:-

KVL in the armature per-phase equivalent circuit:

$$\vec{E}_A = R_A \vec{I}_A + jX_s \vec{I}_A + \vec{V}_\phi$$

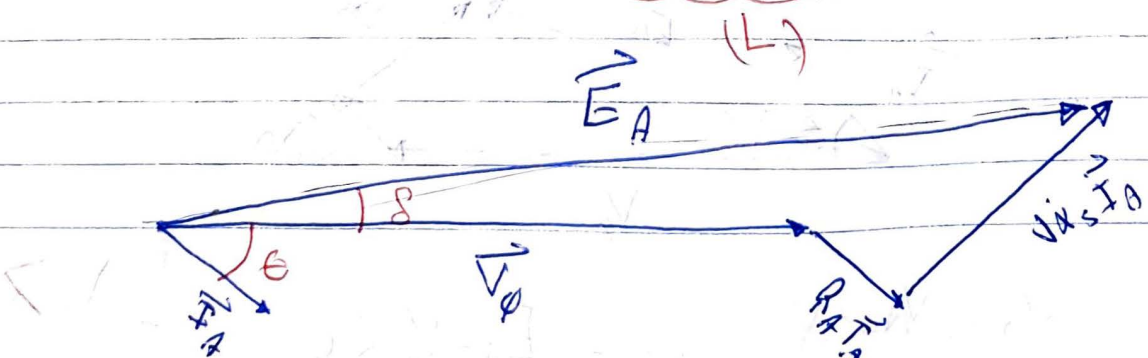
⊗ Phasor Diagram

$$\vec{E}_A = \vec{V}_\phi + R_A \vec{I}_A + jX_s \vec{I}_A$$

⊗ Assume that the Reference angle of \vec{V}_ϕ is zero

$$\Rightarrow \vec{V}_\phi = V_\phi \angle 0^\circ$$

⊙ Lagging PF operation \Rightarrow The SG is connected to an inductive load.



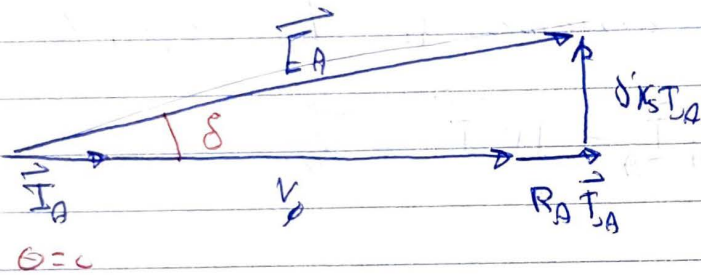
$$V_\phi < E_A$$

$\theta \Rightarrow$ PF angle
 $\delta \Rightarrow$ Torque angle (angle between $\vec{V}_\phi + \vec{E}_A$)

$$\text{Voltage Regulation} = V_R = \frac{V_{NL} - V_{FL}}{V_{FL}} \times 100\%$$

$$V_R = \frac{E_A - V_\phi}{V_\phi} \times 100\% > 0$$

(2) unity PF \Rightarrow The generator is connected to a resistive load (R)

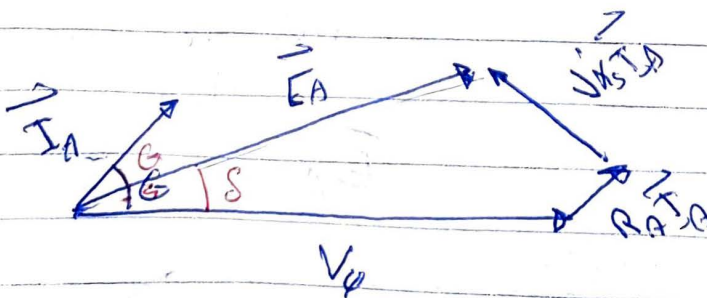


$$V_\phi < E_A$$

$$V_R = \frac{V_{NL} - V_{FL}}{V_{FL}} \times 100\% = \frac{E_A - V_\phi}{V_\phi} > 0$$

$$V_{R_{\text{unity}}} < V_{R_{\text{leading}}}$$

(2) Leading PF \rightarrow The generator is connected to a capacitive load (C)



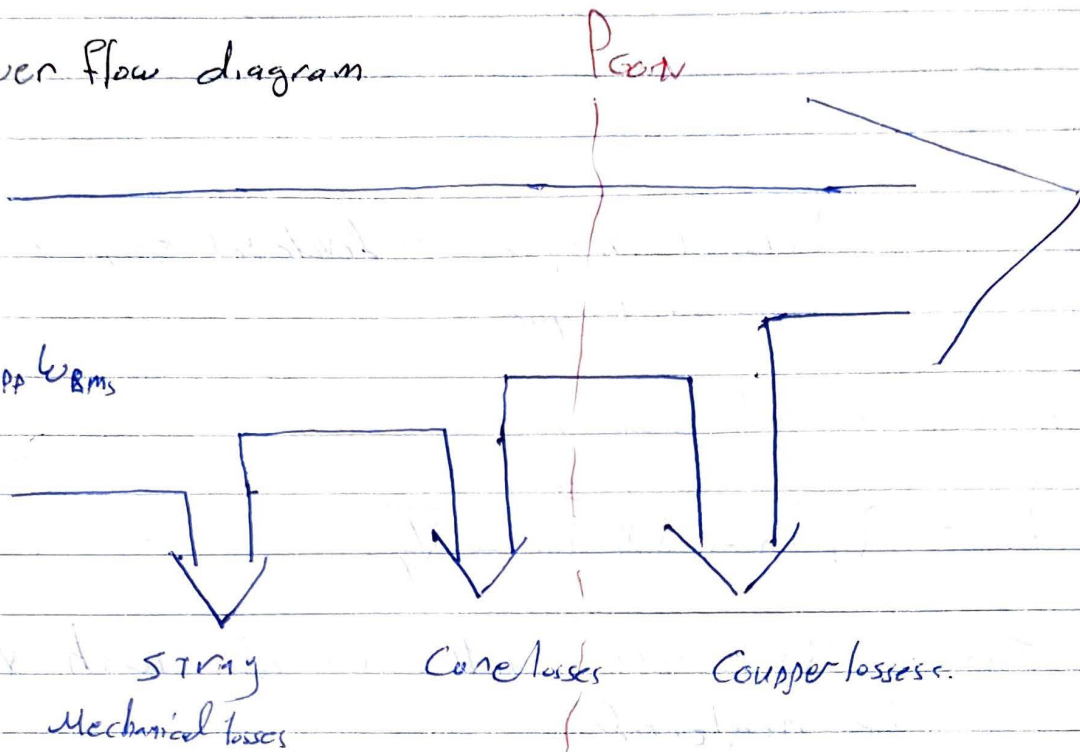
$$V_R = \frac{V_{NL} - V_{FL}}{V_{FL}} \times 100\% = \frac{E_A - V_\phi}{V_\phi} < 0$$

$$[V_\phi > E_A]$$

Power and Torque equations.

- Power flow diagram

$$P_{in} = T_{app} \omega_{RMS}$$



$$P_{out} = 3 V_{\phi} I_{\phi} \cos \theta = \sqrt{3} V_L I_L \cos \theta$$

$$Q_{out} = 3 V_{\phi} I_{\phi} \sin \theta = \sqrt{3} V_L I_L \sin \theta$$

Y-connection

Δ -connection

$$V_L = \sqrt{3} V_{\phi}$$

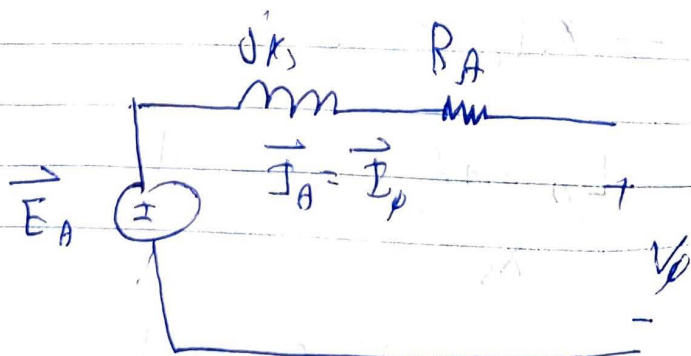
$$I_L = I_{\phi}$$

$$V_L = V_{\phi}$$

$$I_L = \sqrt{3} I_{\phi}$$

T_{app} : Applied Torque

ω_{RMS} : Synchronous speed.



3- ϕ

$$P_{\text{conv}} = T_{\text{ind}} \omega_{ms} = 3 E_A I_A \cos \delta$$

power converted
into electrical

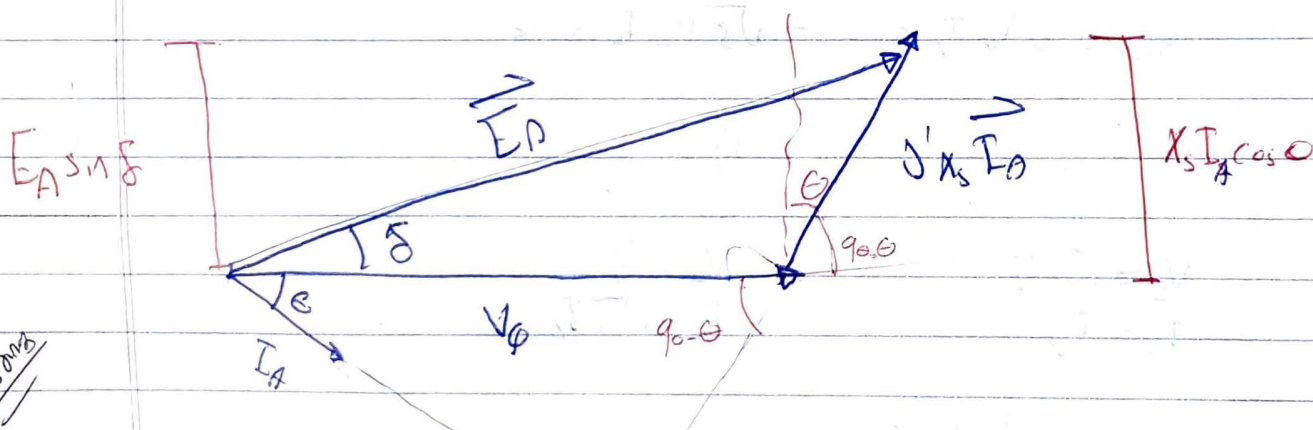
T_{ind} = Induced torque, or developed torque or electro magnet torque

⊕ Assume that the generator is connected to 3- ϕ inductive load

$$\vec{E}_A = R_A \vec{I}_A + jX_s \vec{I}_A + \vec{V}_\phi$$

Since R_A is very small compared with X_s its can be neglected.

$$\vec{E}_A = jX_s \vec{I}_A + \vec{V}_\phi$$



From the phasor diagram

$$E_A \sin \delta = X_s I_A \cos \theta$$

$$\Rightarrow I_A \cos \theta = \frac{E_A \sin \delta}{X_s} \quad \times 3V_\phi$$

P_{conv} vs des eq

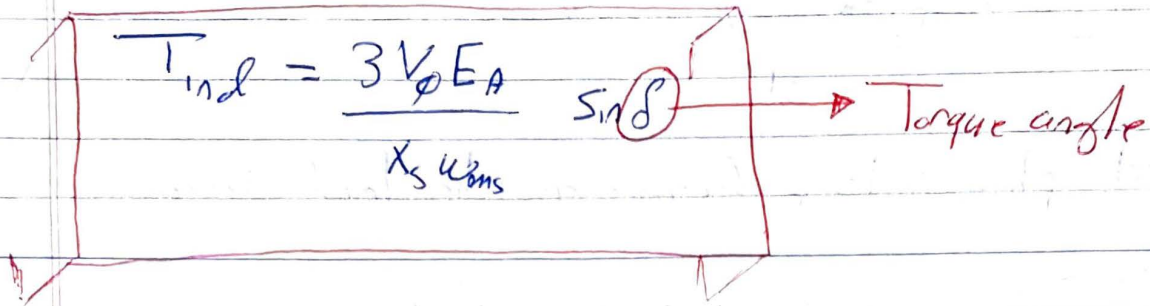
$$3 V_\phi I_A \cos \theta = \frac{3 V_\phi E_A \sin \delta}{X_s}$$

$$\Rightarrow P_{out} = 3V_{\phi} I_A \cos \theta = \frac{3V_{\phi} EA}{X_s} \sin \delta = P_{conv}$$

R_A is ignored

$$P_{conv} = T_{ind} \omega_{ms} = \frac{3V_{\phi} EA}{X_s} \sin \delta$$

Machine Rated δ
0.8590



The maximum output power is ω_c .

$$P_{max} = \frac{3V_{\phi} EA}{X_s} \Rightarrow \sin \delta = 1 \Rightarrow \delta_{max} = 90^\circ$$

(0.8590)

↳ This is the steady state stability limit.

Effect of load changes on SG operation.

Assume that - SG is connected to a 3 ϕ inductive load

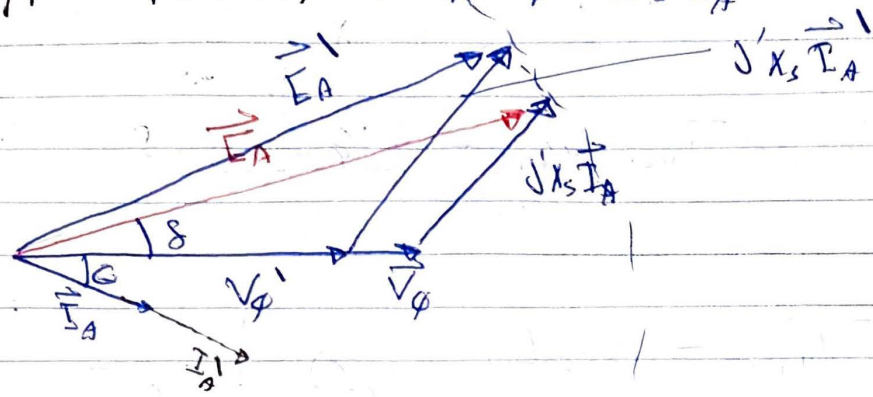
- $E_A = \text{constant}$ speed of prime mover = constant
 Machine flux = constant

- R_A is ignored

- load increases at the same PF angle

□

① Lagging PF operation, $E_A = \vec{V}_\phi + jX_s \vec{I}_A$

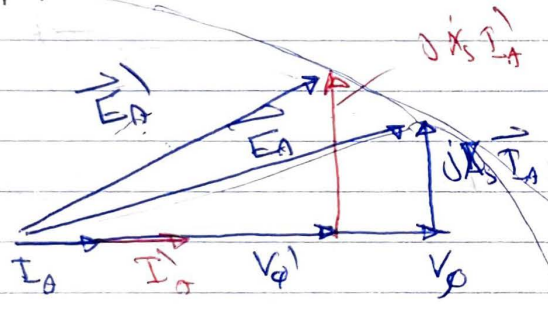


The phase voltage decreases as the load increases

AVR or Automatic Voltage Regulator

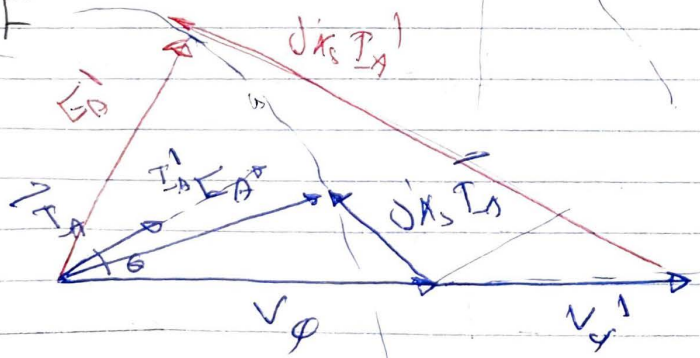
↳ its a closed loop controller to keep the phase voltage of generator constant.

② unity PF



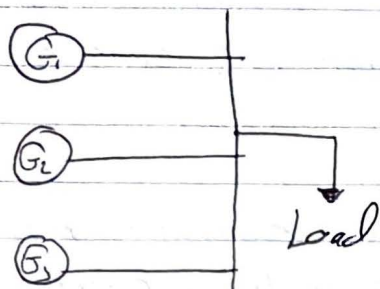
V_ϕ decreases as the load increases.

③ leading PF



Parallel operation of Synchronous Generators

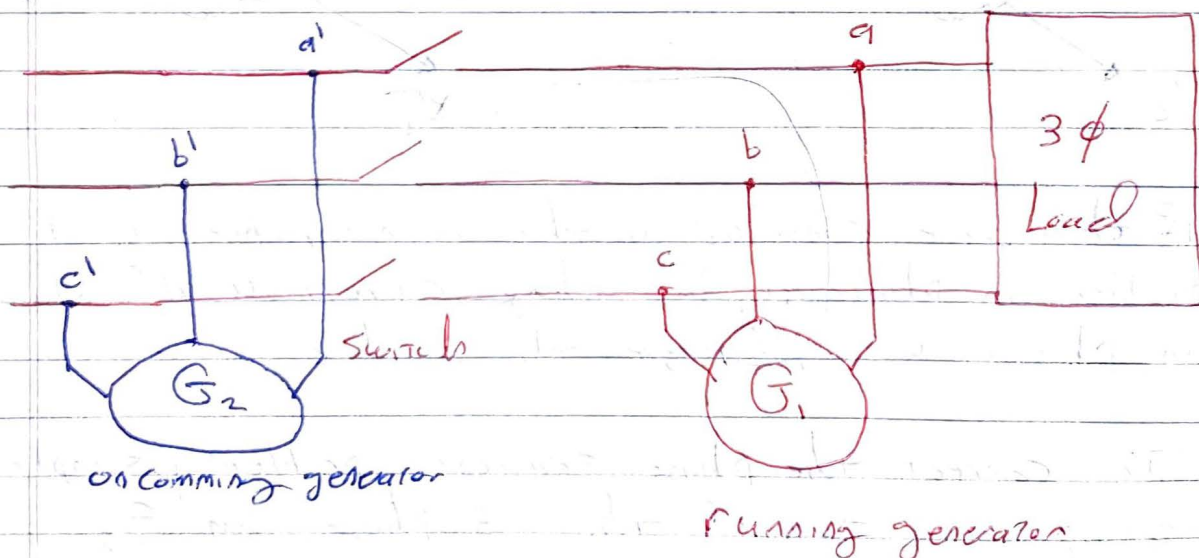
Other than emergency generator, rarely there is a case where a single/isolated generator supplies a load.



Major advantages

- 1) supplies a larger load
- 2) high reliability of power system
- 3) Allows one or more generator to be removed for shutdown & preventive maintenance.
- 4) if only one generator is used and it's run running of full-load, it's a very inefficient process.

Conditions required for paralleling.



- 1) The generator ^{must} have the same Rms line Voltage

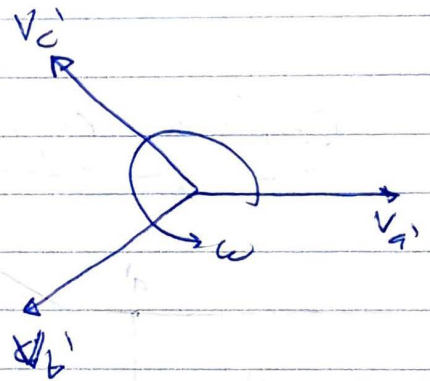
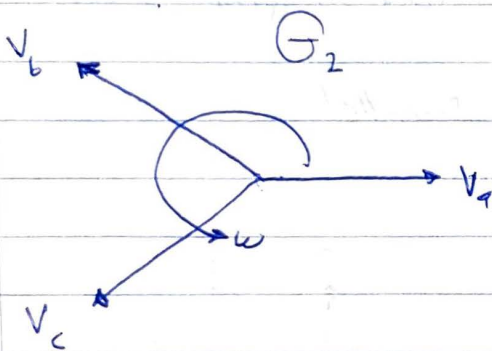
2) The generator, must have the same phase sequence.

3) The phase angle of two "a" phases, "b" phases or "c" phases must be the same.

4) The frequency of the incoming generator must be slightly higher than the frequency of running generator.

Point ① → The RMS line voltages of the two generators must be the same to avoid any huge circulating current flowing the phases and damaging the generator.

Point ② → Assume the generators have an opposite phase sequence.



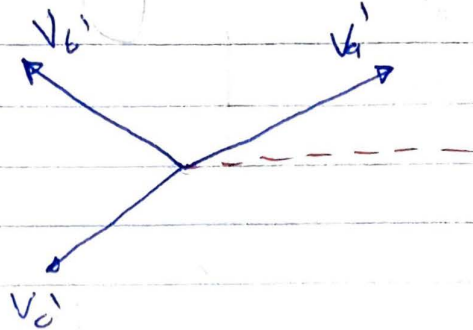
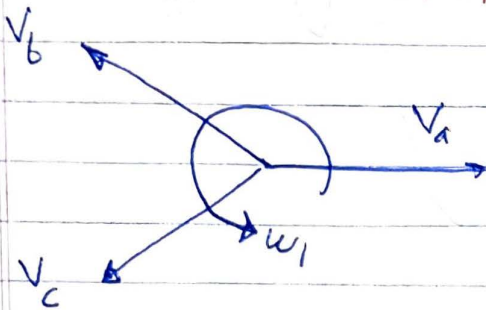
⊗ if they were connected in this manner, there would no problem in phase (a), but a huge current would flow in phases b & c, damaging the machine.

Solution →

To correct the phase sequence problem, simply swap any two of the 3 phases on G_2 .

Point 384 ω_1 Assume that the frequency of G_1 is $\omega_1 = 2\pi f_1$, and the frequency of G_2 is $\omega_2 = 2\pi f_2$

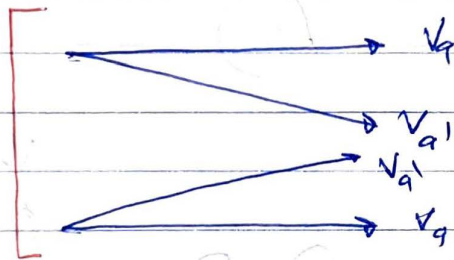
Assume that $\omega_2 > \omega_1$



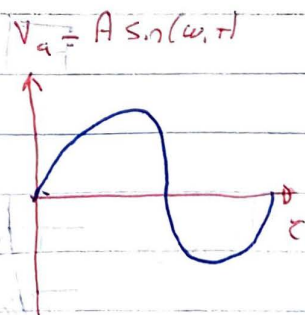
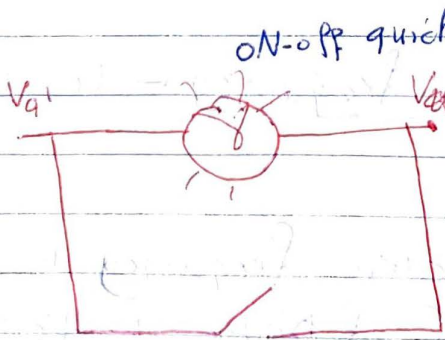
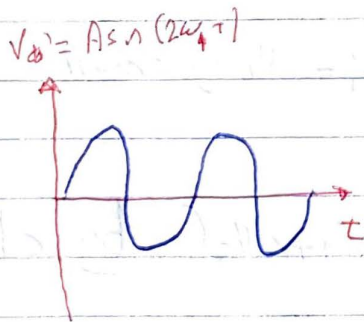
"In phase"



"OUT of phase"



Case 1 $\omega_1 \neq \omega_2$, but the difference is high



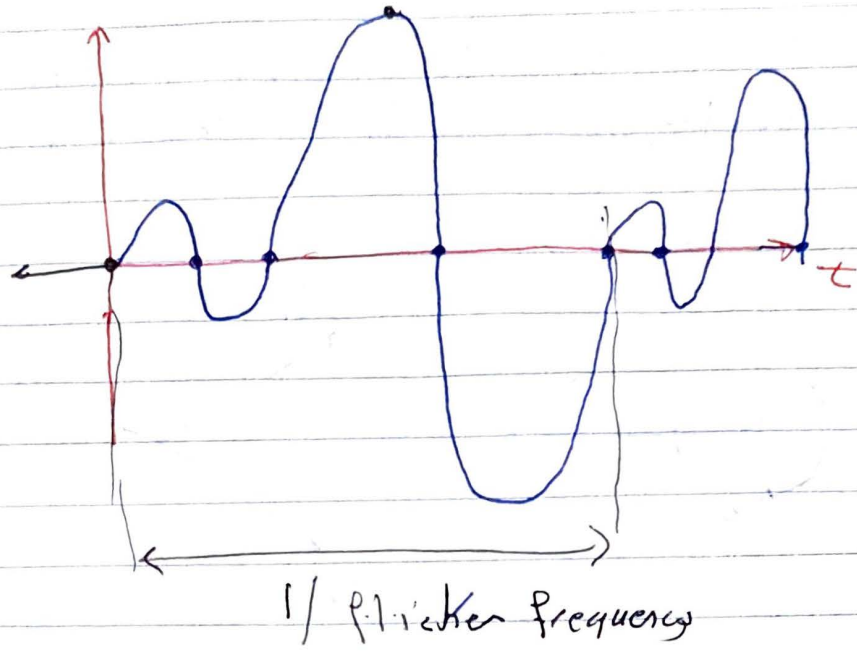
$$PD = V_a - V_{a'}$$

⊗ Potential difference

$$\text{Flicker frequency} = \omega_2 - \omega_1 = \omega$$

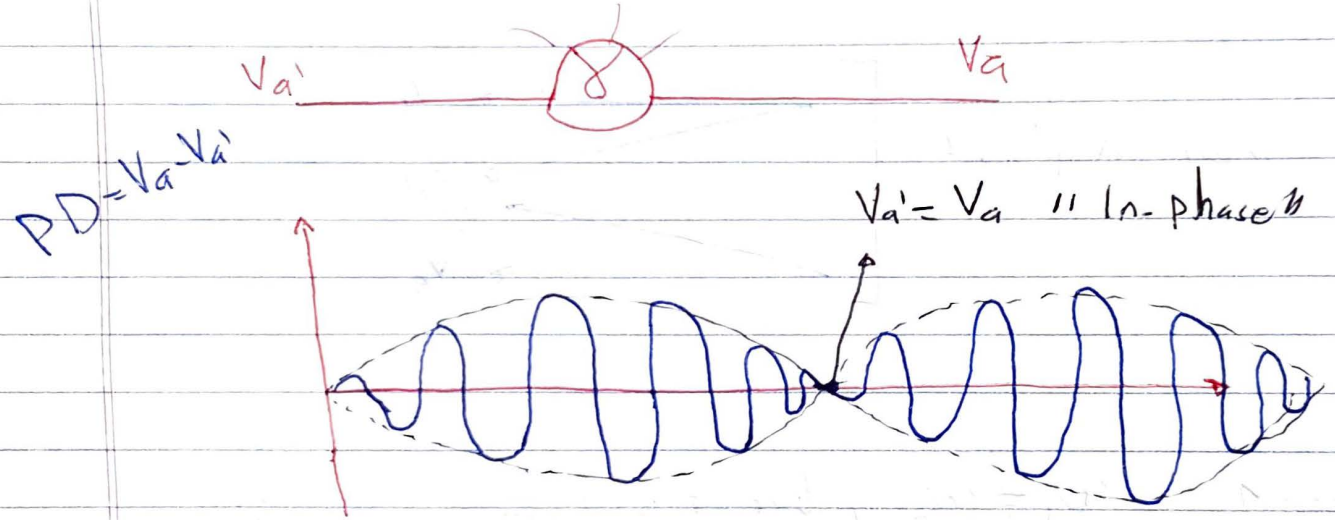
120 out of 1 phase

$V_a = V_{a'}$
in phase



Case 2

$\omega_1 \neq \omega_2$ but the difference is very small

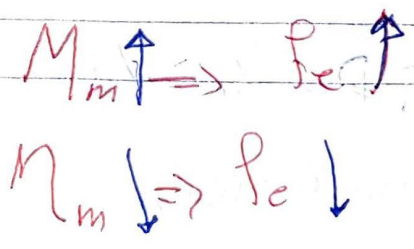


Flicker Frequency = $\omega_2 - \omega_1$ = very small

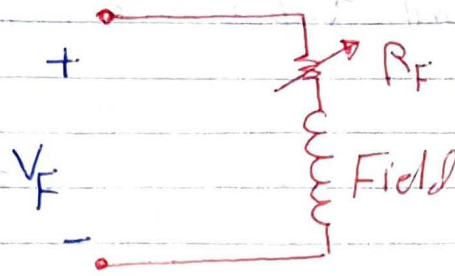
Notes

The electric frequency is controlled by changing the speed of prime mover

$$M_m = \frac{120 f_e}{P}$$



Note: The terminal voltage is controlled by changing the field current.

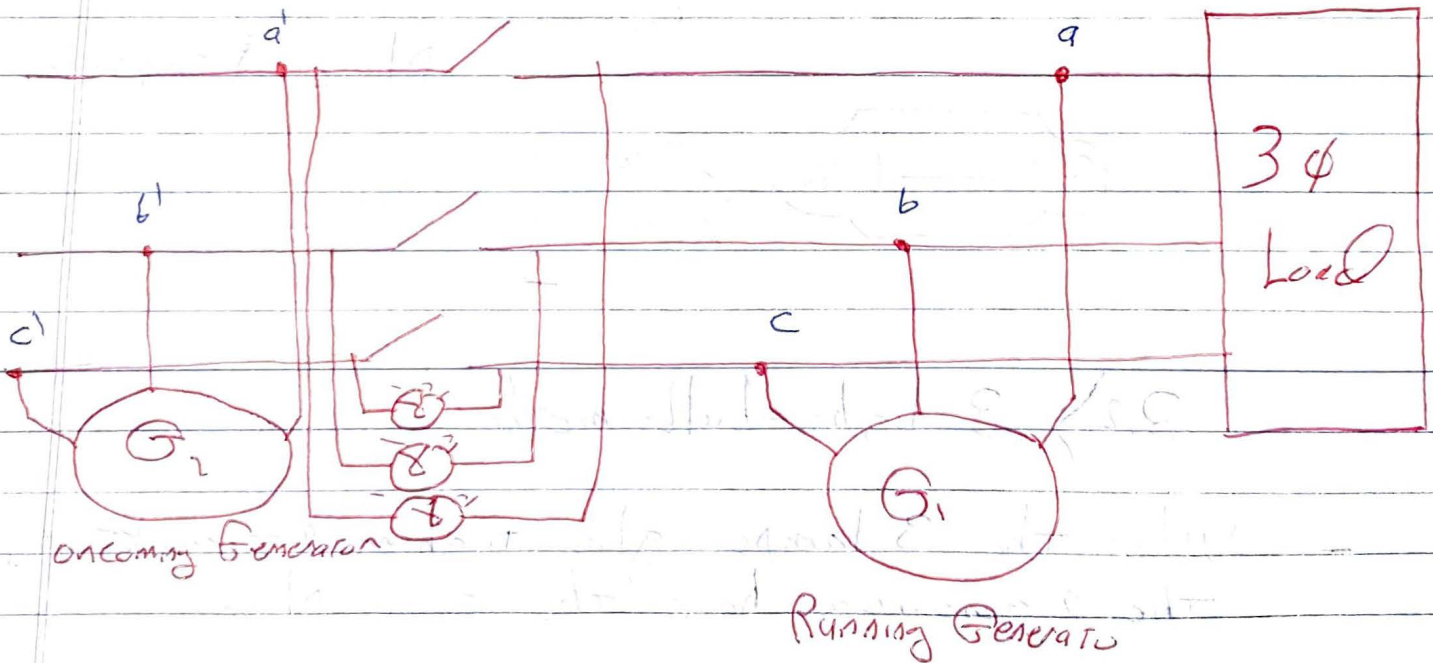


$$R_F \uparrow \Rightarrow (I_F = \frac{V_F}{R_F}) \downarrow \Rightarrow \phi \downarrow \Rightarrow E_A \downarrow \Rightarrow V_{\phi} \downarrow$$

$$R_F \downarrow \Rightarrow I_F \uparrow \Rightarrow \phi \uparrow \Rightarrow E_A \uparrow \Rightarrow V_{\phi} \uparrow$$

⊗ procedure of synchronizing

Switches

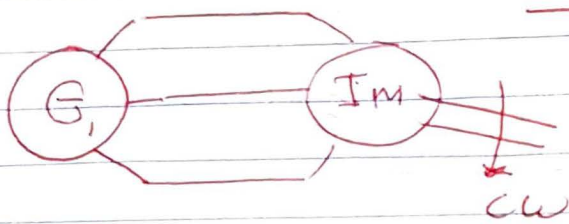


- 1) Adjust the speed of G_2 to match that of G_1 .
- 2) Using voltmeters, adjust I_F of G_2 to make the (V_T) terminal voltage of G_2 equals the terminal rms voltage of G_1 .

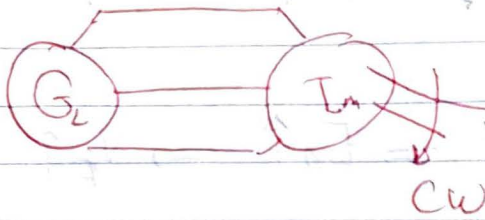
$V_T =$ Terminal line Voltage

3) phase-sequence

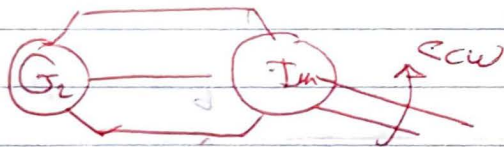
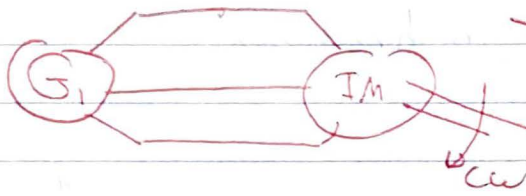
3.1) small 3- ϕ induction motor method.



They have
the same phase
sequence.



They have opposite
phase & sequence.

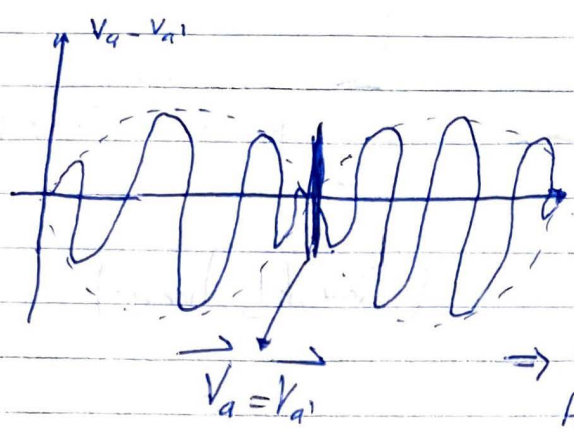


3.2) 3 light-bulbs method.

- When the 3 lamps glow together & turn off together
The 2 generators have the same phases

- When the 3 lamps glow in succession, then the
2 generator have opposite phase sequence.

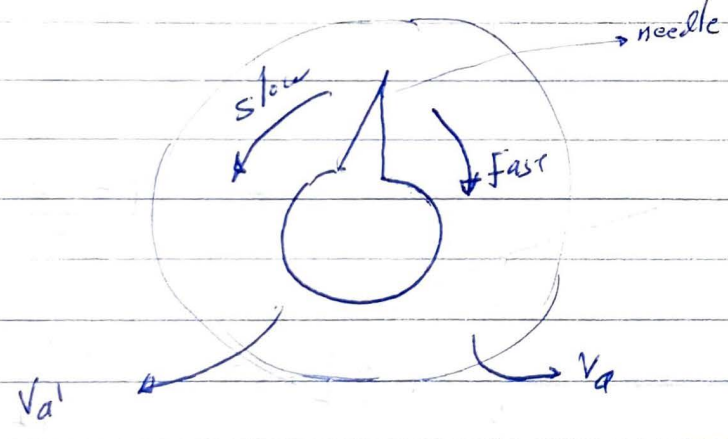
4) Frequency of G_2 is slightly higher than the frequency of G_1 .



when the 3 lamps go out V_a & $V_{a'}$ are in phase, and paralleling can be done.

⇒ This method is not very accurate. A better method should be used (synchroscope).

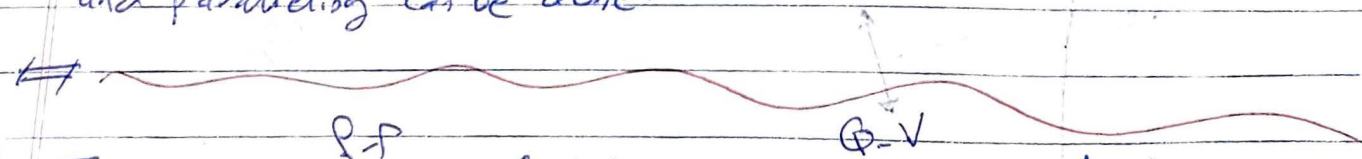
Synchroscope → Device that gives an indication about the phase shift between V_a & $V_{a'}$.



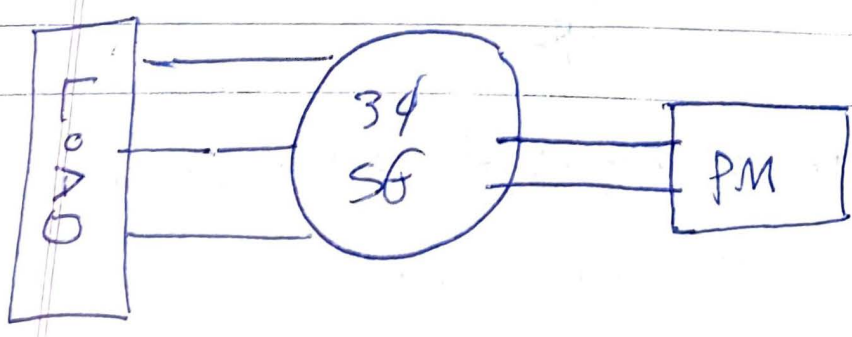
$f_2 > f_1 \Rightarrow$ CW Rotation (Fast)

$f_2 \approx f_1 \Rightarrow$ CW Rotation (slow)

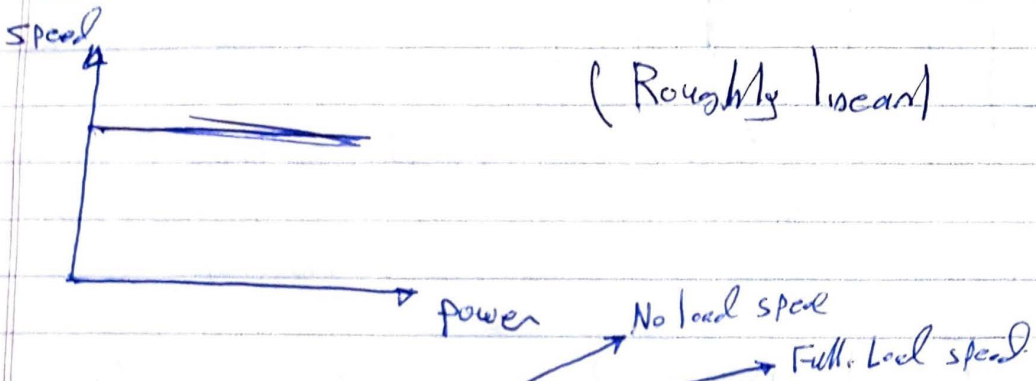
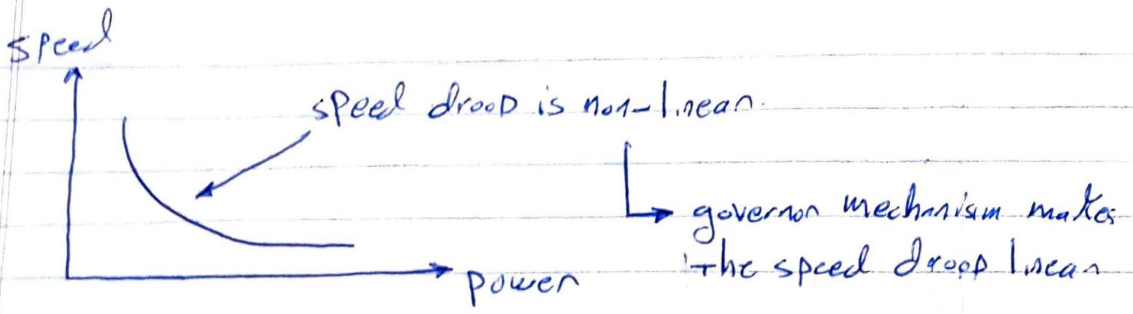
When the needle is in the vertical position, V_a is in phase with $V_{a'}$ and paralleling can be done.



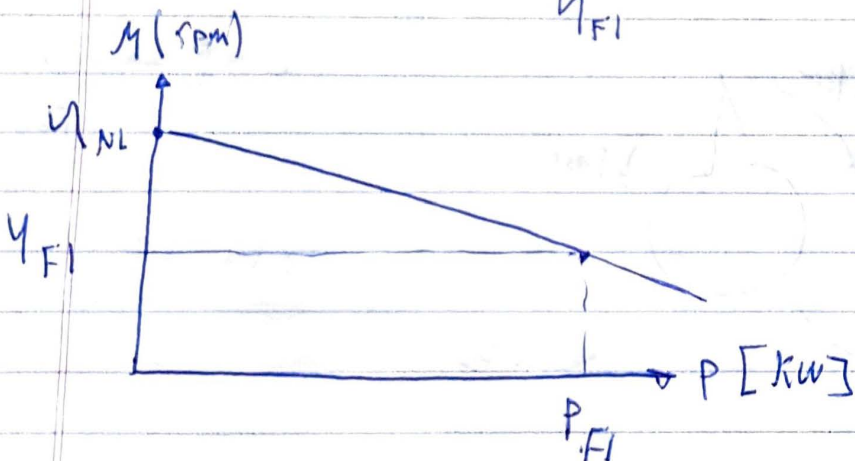
Frequency-power and Voltage-reactive power characteristics of generator.



- wind turbine
- water turbine
- Diesel steam engine

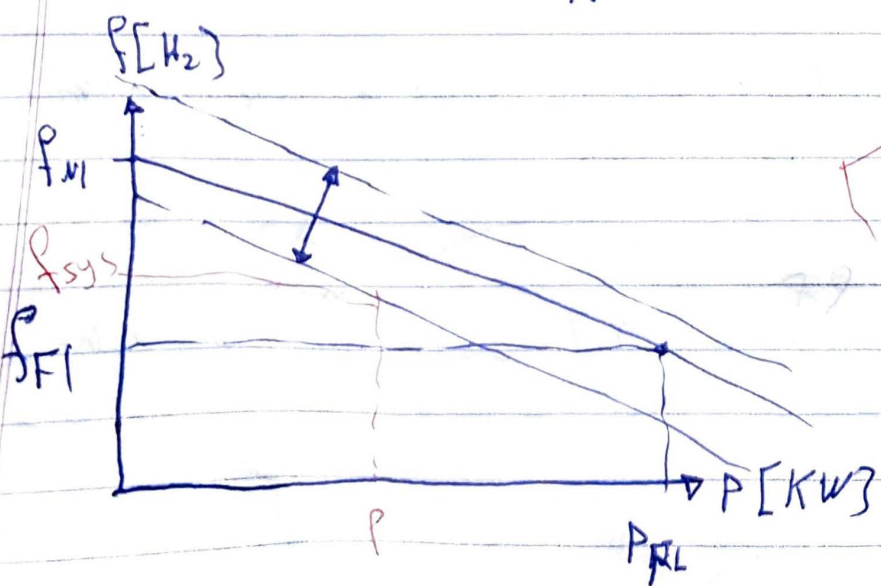


Speed Droop = $SD = \frac{\omega_{NL} - \omega_{FL}}{\omega_{FL}} \times 100\%$



$\omega = \frac{120}{P} f$

$f = \frac{n P}{120}$



Speed governor

By adjusting the setpoint of the speed governor, we can increase or decrease the no load speed.

$$\text{slop} = \frac{g_2 - g_1}{x_2 - x_1} = \frac{P_{FI} - P_{NL}}{P_{FI}} \quad [\text{Hz/KW}]$$

$$P_{FI} = \frac{1}{\text{slop}} [P_{FI} - P_{NL}] = \frac{1}{\text{slop}} [P_{NL} - P_{FI}]$$

In general,
$$P = S_p [f_{NL} - f_{\text{sys}}]$$

System frequency

where S_p is the power slop $[\text{KW/Hz}]$.

⊗

Voltage-Reactive Power characteristic

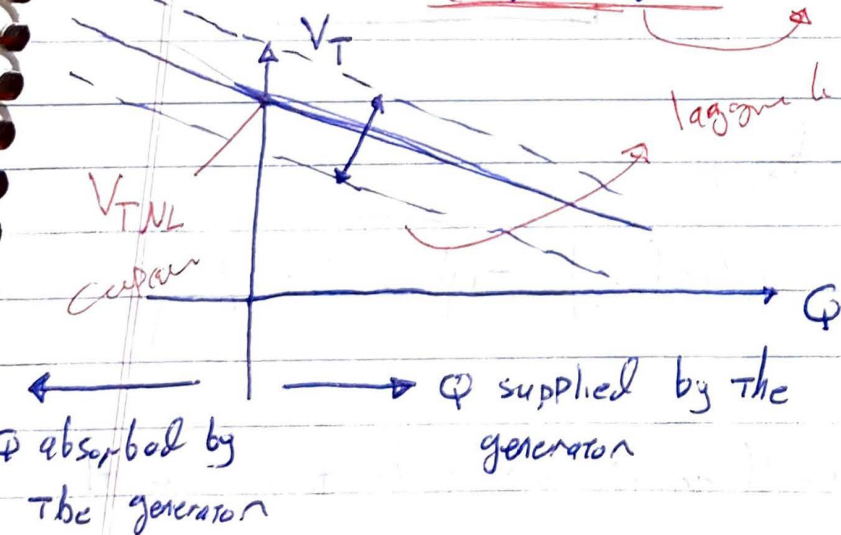
$$S_p = \frac{(P)_{\text{max}}}{S_{NL} - P_{FI}}$$

lagging load $\uparrow \Rightarrow$ The load absorbs more ϕ

\Rightarrow The generation supplies more $\phi \Rightarrow V_T \downarrow$

\Rightarrow The characteristic is non-linear

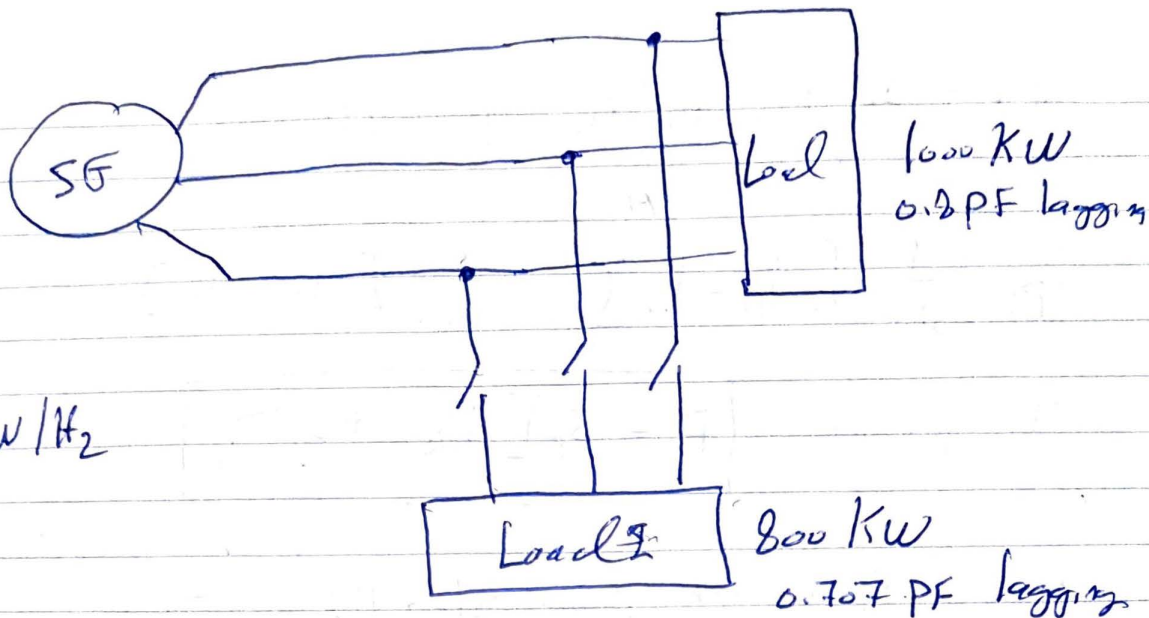
\Rightarrow The AC voltage regulation makes it linear.



AC Voltage Regulation

By adjusting the set points of the AC voltage regulator we can increase or decrease the no-load terminal voltage

Example



$$P = 61 \text{ Hz}$$

$$S_P = 1 \text{ MW/Hz}$$

a) before the switch is closed, what is the operating frequency of the system

b) After, load 2 is connected, what is the operating frequency of the system

Solution

$$a) P = S_P (P_{NL} - P_{sgs})$$

$$1000 = 1000 (61 - f_{sgs}) \Rightarrow f_{sgs} = 60 \text{ Hz}$$

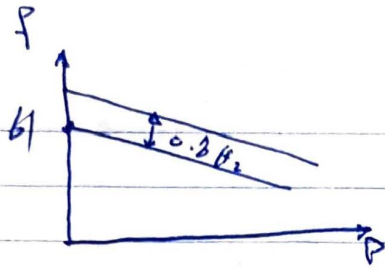
$$b) P = S_P (P_{NL} - P_{sgs})$$

$$1000 + 800 = 1000 (61 - f_{sgs}) \Rightarrow f_{sgs} = 59.2 \text{ Hz}$$

c) what action could an operator take to restore the system frequency.

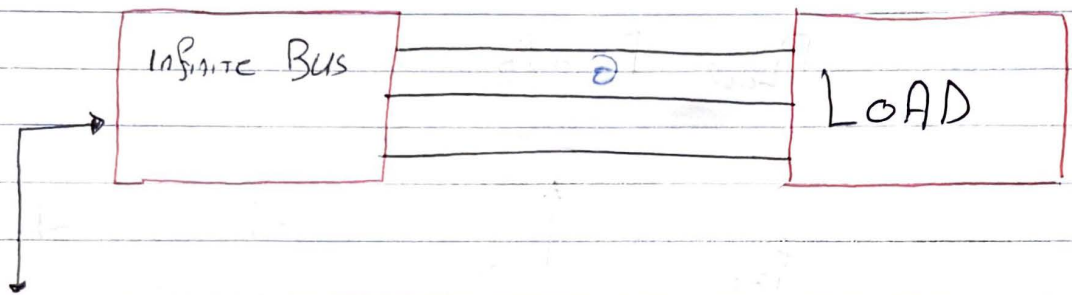
$$P = S_P (P_{NL} - P_{sgs})$$

$$1000 + 800 = 1000 (P_{NL} - 60) \Rightarrow P_{NL} = 61.8$$

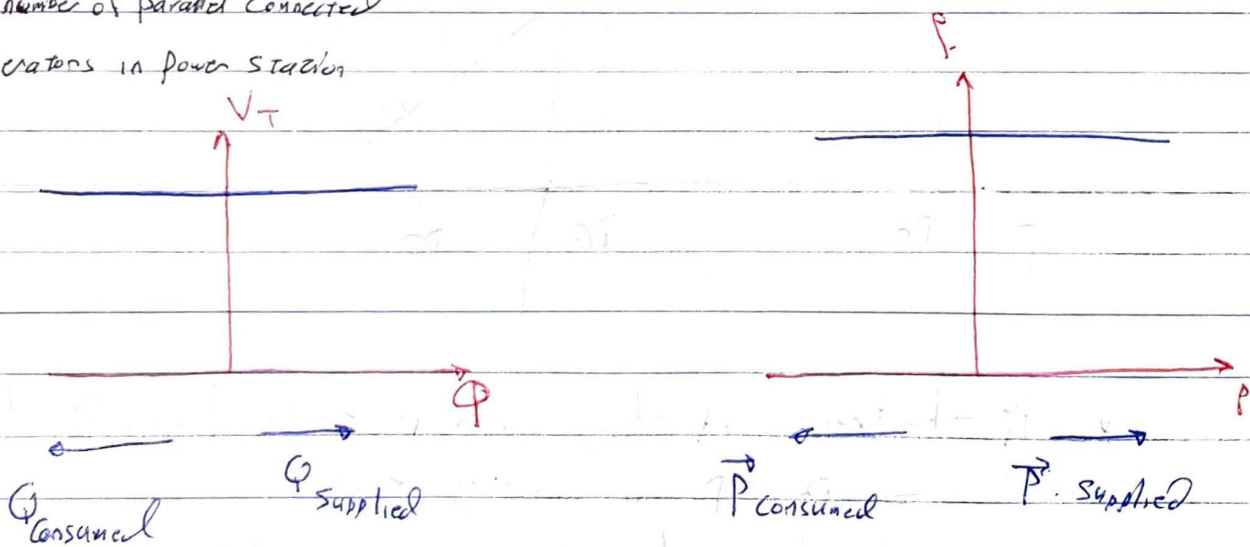


⊕ Parallel operation of Generators with large power system

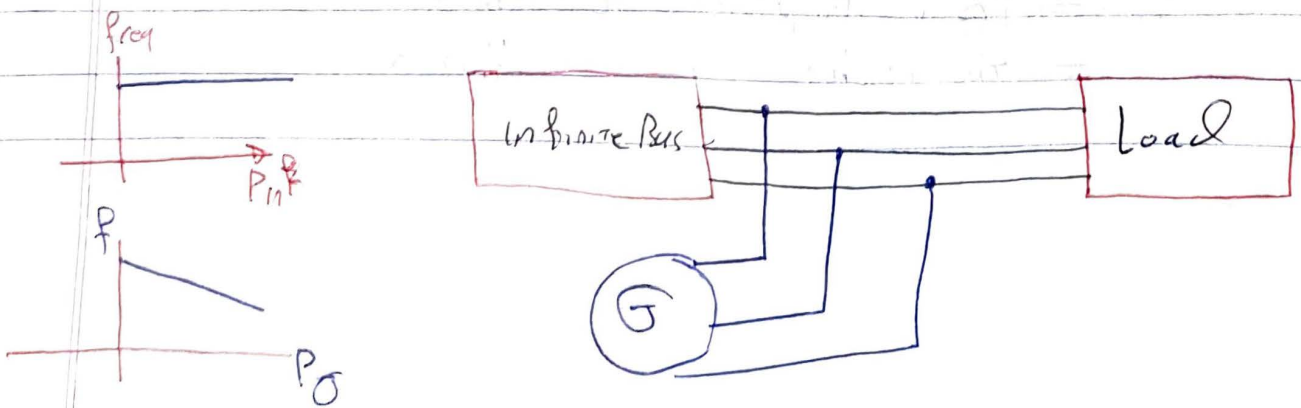
Infinite Bus: it is a large power system that its voltage and frequency do not vary regardless of how much power are drawn from or supplied to it.

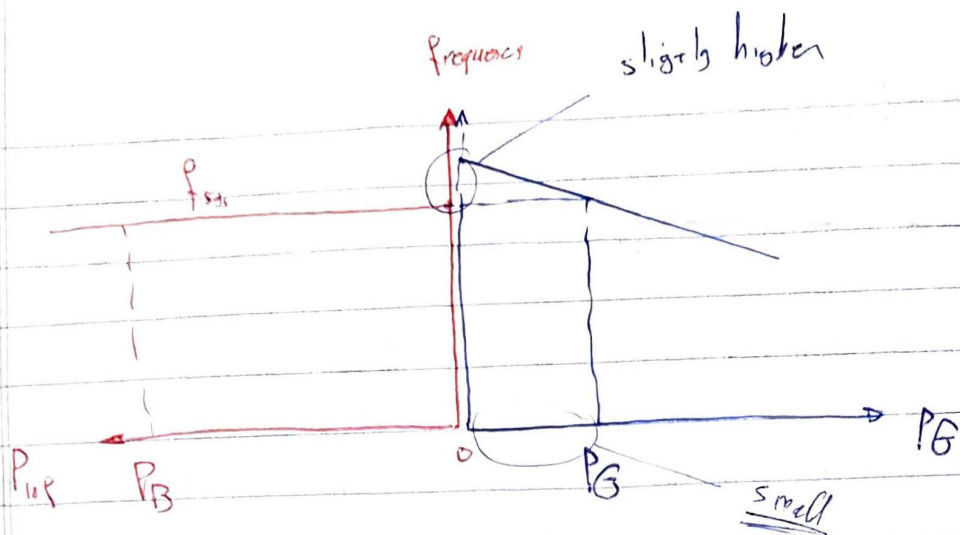


high number of parallel connected generators in power station



⊕ Parallel operation

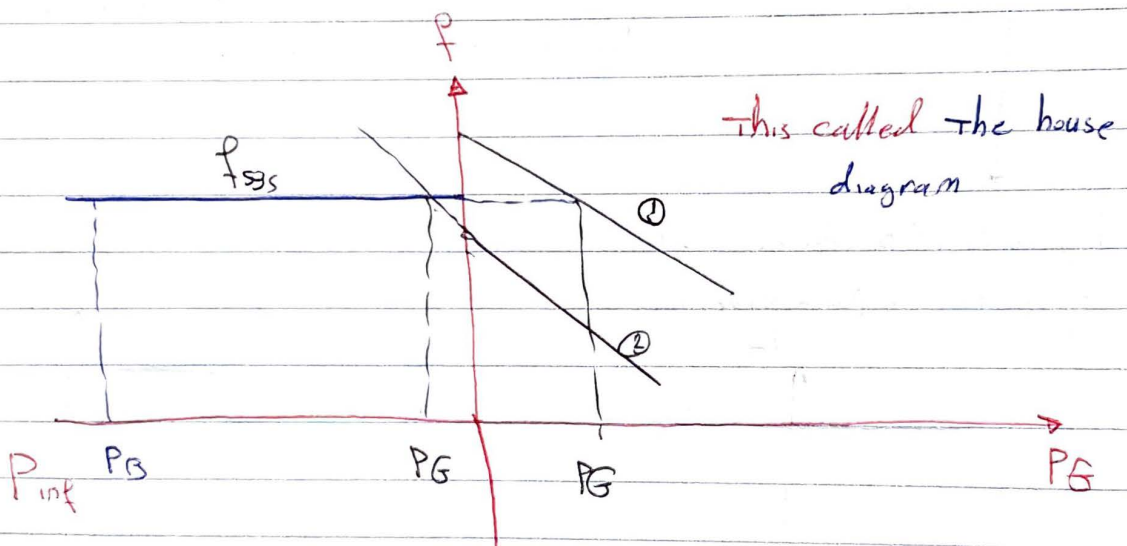




P_B : Power supplied by infinite Bus

P_G : Power supplied by the generator.

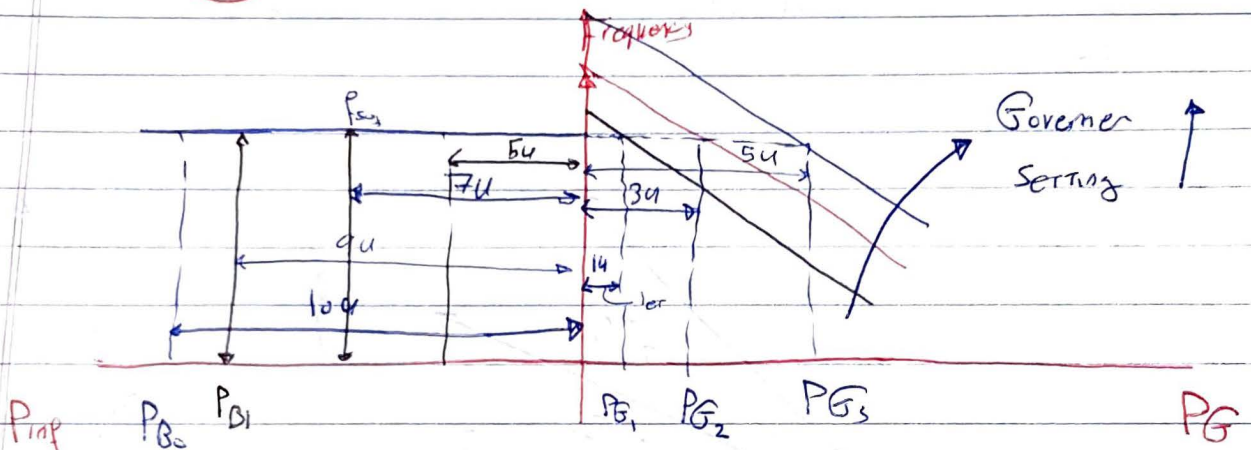
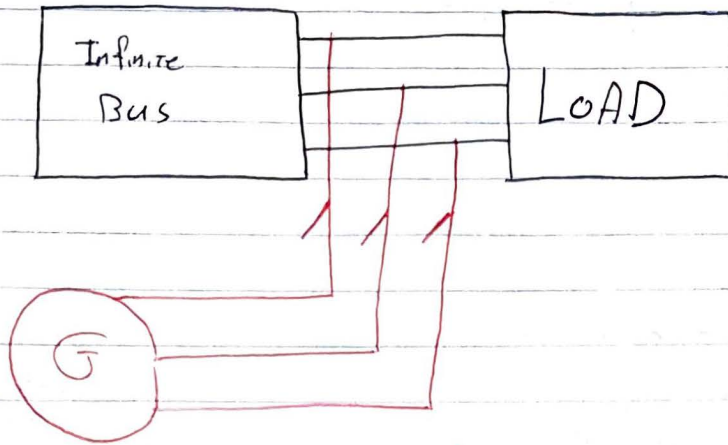
$$P_{Load} = P_G + P_B$$



* if The frequency of the generator is slightly higher ① than $f_{sys} \Rightarrow P_G$ is positive and very small \Rightarrow the machine acts as a generator.

⊙ if The frequency of generator is slightly lower ② than $f_{sys} \Rightarrow P_G$ is negative & very small \Rightarrow the machine acts as Motor.

* Increasing of governor setting



Before synchronizing $\Rightarrow P_{B_0} = 104, P_{G_0} = 0 \Rightarrow P_{Load} = P_{B_0} + P_{G_0} = 104$

After synchronizing $\Rightarrow P_{B_1} = 94, P_{G_1} = 10 \Rightarrow P_{Load} = P_{B_1} + P_{G_1} = 104$

Governor setting $\uparrow \Rightarrow P_G \uparrow \& P_B \downarrow \Rightarrow P_{G_2} = 34 \& P_{B_2} = 74$

$$\Rightarrow P_{Load} = P_{G_2} + P_{B_2} = 104$$

Governor setting $\uparrow \uparrow \Rightarrow P_G \uparrow \uparrow \& P_B \downarrow \downarrow \Rightarrow P_{G_3} = 54 \& P_{B_3} = 54$

$$P_{Load} = P_{G_3} + P_{B_3} = 104$$

Phasor Diagram

$$P_G = \frac{3V_\phi E_A}{X_s} \sin \delta \rightarrow P_G \propto E_A \sin \delta$$

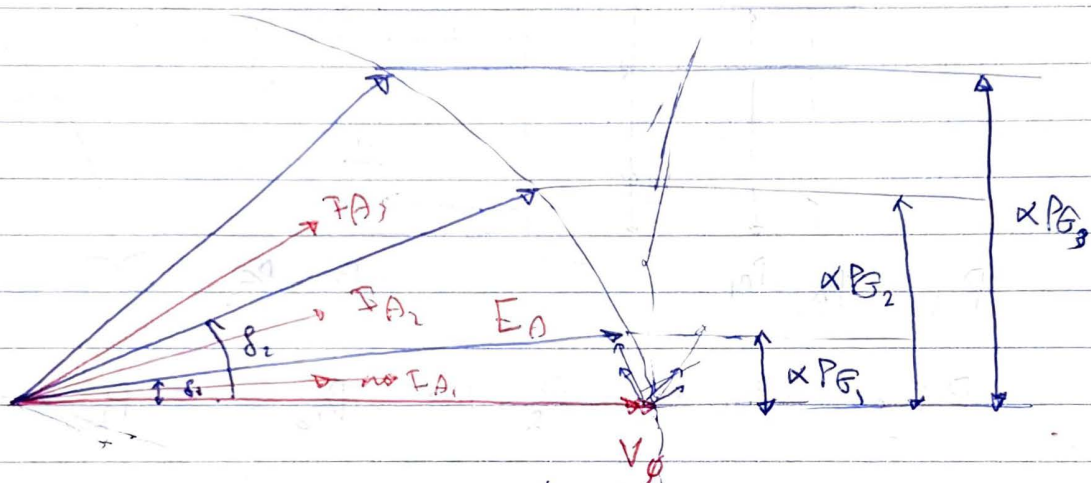
V_ϕ : constant

X_s : constant

$$E_A = K\phi\omega = \text{constant}$$

constant (Infinite Bus)
 (If I_f constant)

$$\vec{E}_A = \vec{V}_\phi + jX_s \vec{I}_A$$



The generator is operating at leading PF
 → seconds as (e)

⇒ The generator supplies a negative reactive power or it consume reactive power from the infinite bus.

- ⊛ How can the generator be adjusted to supply reactive power?
 " by field current adjustment

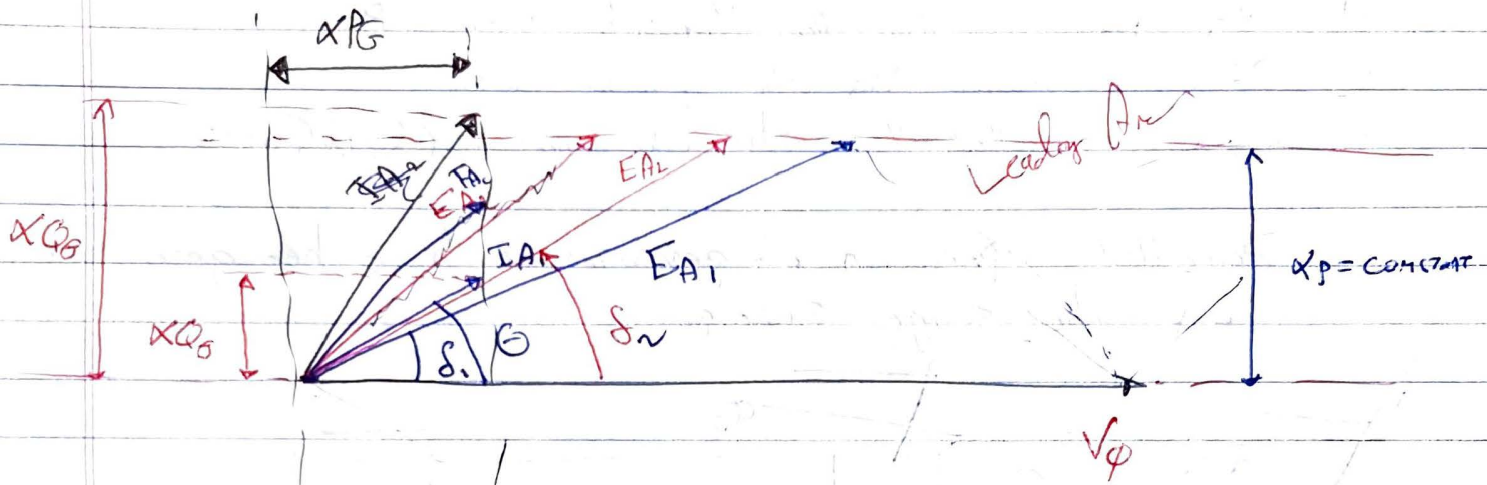
⊛ Adjustment of Reactive Power:

" changing the excitation i.e. field current"

$$P_G = \frac{3 V_\phi E_A \sin \delta}{X_s} = 3 V_\phi I_A \cos \theta = \text{Constant} \quad \text{"by the user"}$$

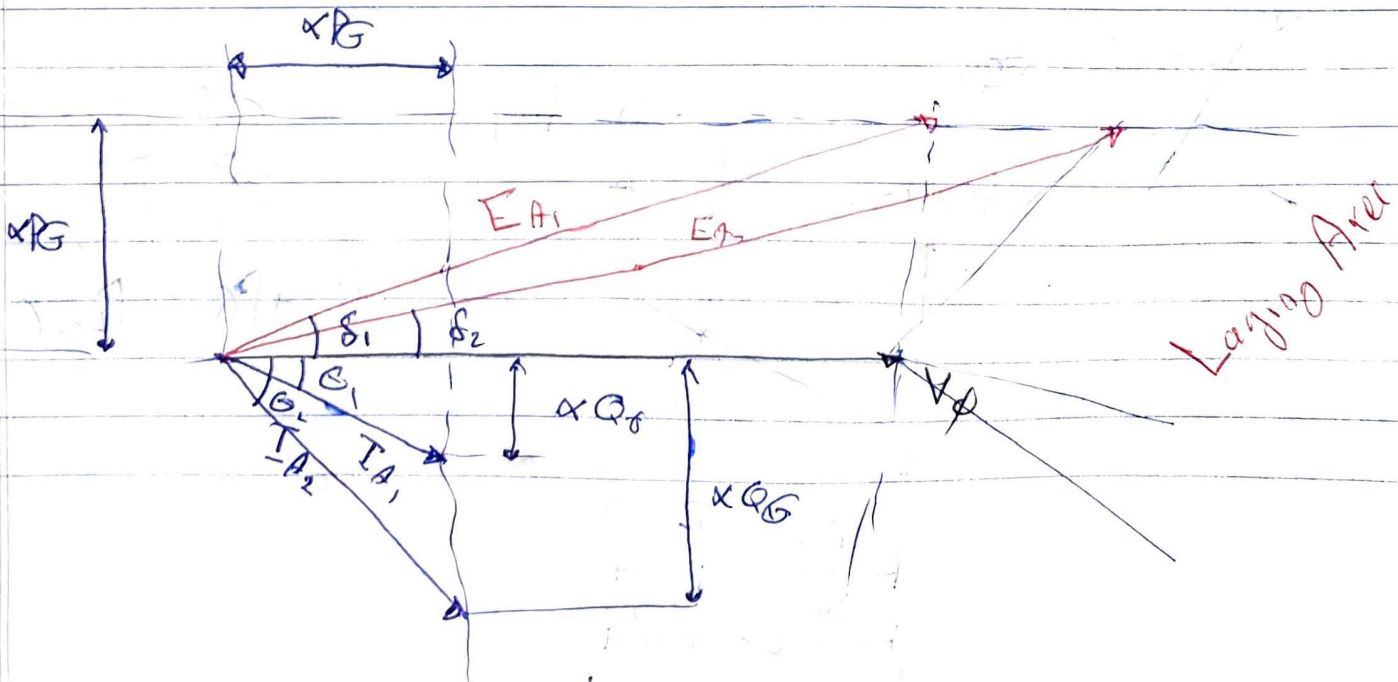
$V_\phi = \text{constant}$ "Infinite Bus"
 $X_s = \text{constant}$ "Infinite Bus"

Since P_G is constant $\Rightarrow E_A \sin \delta = \text{constant}$
 $I_A \cos \theta = \text{constant}$



∴ The Generators absorbed Reactive Power "underexcitation process"

$I_F \downarrow \Rightarrow Q_G \uparrow$ absorbed
 Infinite Bus \rightarrow $\cos \theta$ is constant \rightarrow I_F is variable \rightarrow δ is variable



⊗ changing the excitation (field current)

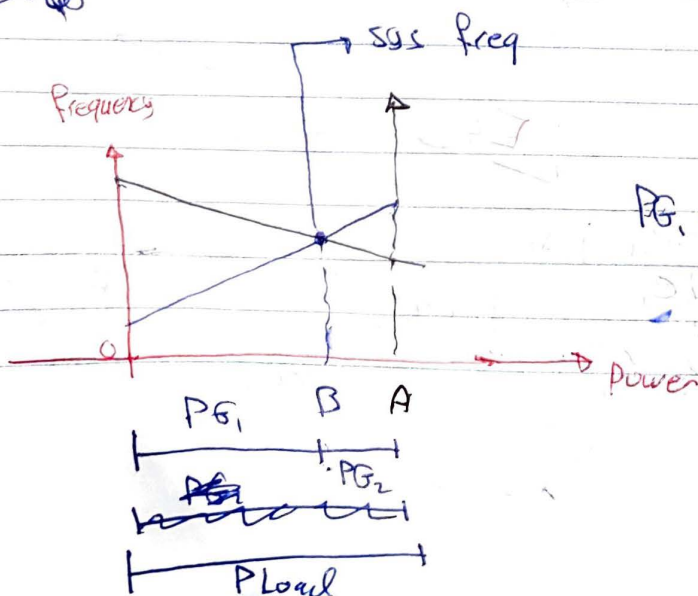
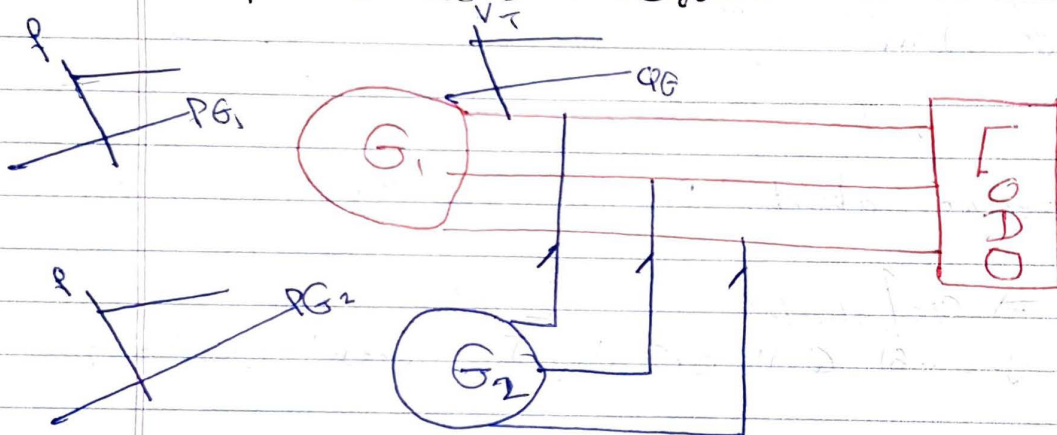
$$I_F \uparrow \Rightarrow Q_G \uparrow_{\text{supplied}}$$

Lagging Area → The generator supplies reactive power "over-excitation"

Conclusion

- ① V_T & f_{sys} are controlled via the infinite bus.
- ② P_G is controlled via the governor setting.
- ③ Q_G is controlled via the excitation. (field current)

Parallel operation of generator with other generators of the same size



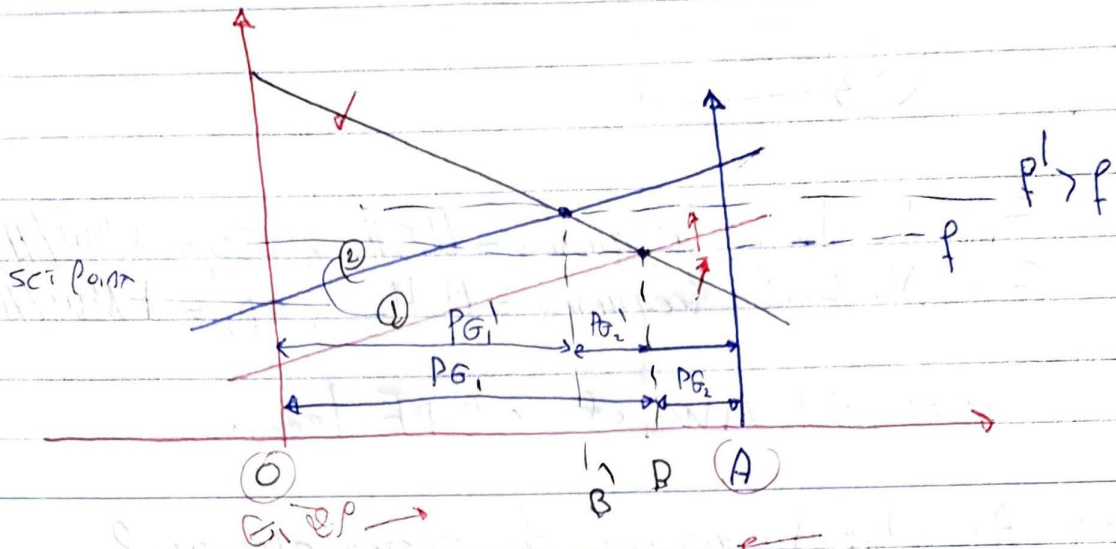
OA: P_{Load}

OB: P_{G1}

BA: P_{G2}

$$P_{G1} + P_{G2} = P_{\text{Load}}$$

changing The governer setting.



$$OB' = PG_1' \quad \text{at } \textcircled{1}$$

$$B'A = PG_2' \quad \text{at } \textcircled{2}$$

$$OA = P_{Load}$$

$$OB = PG_1 \quad \text{at set point II}$$

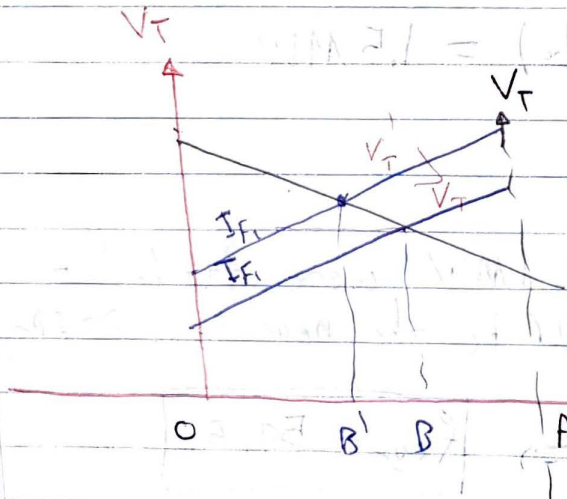
$$BA = PG_2 \quad \text{at set point I}$$

Governer setting of $G_2 \uparrow$

$$f_{sys} \uparrow \quad PG_1 \downarrow, PG_2 \downarrow$$

$$PG_1 + PG_2 = P_{Load}$$

changing the excitation



$$OA = P_{Load}$$

$$OB = PG_1$$

$$BA = PG_2$$

$$OB' = PG_1' \quad \text{at } IF_2$$

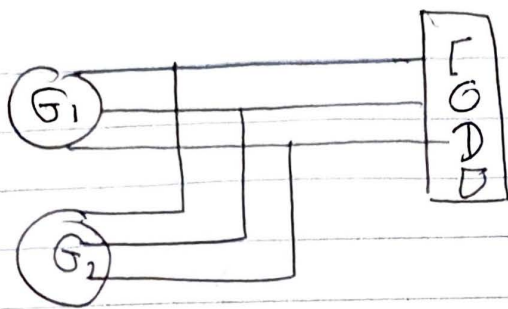
$$B'A = PG_2' \quad \text{at } IF_1$$

$$OA = P_{Load} = PG_1' + PG_2'$$

$$\text{Excitation of Generator } \uparrow \Rightarrow V_T \uparrow \rightarrow PG_1 \downarrow + PG_2 \uparrow$$

Example

Q1



G_1 : No load frequency = 61.5 Hz , $SP_1 = 1 \text{ MW/Hz}$
 G_2 : No load frequency = 61 Hz , $SP_2 = 1 \text{ MW/Hz}$

Load 2.5 MW of 0.8 PF lagging

a) At what frequency is the system operating?

$$P_{G_1} = SP_1 (f_{NL_1} - f_{sys})$$

$$P_{G_2} = SP_2 (f_{NL_2} - f_{sys})$$

$$P_{G_1} + P_{G_2} = 2.5 \Rightarrow \boxed{f_{sys} = 60 \text{ Hz}}$$

b) How much power is supplied by $G_1 + G_2$?

$$P_{G_1} = SP_1 (61.5 - 60) = 1.5 \text{ MW}$$

$$P_{G_2} = 1 \text{ MW}$$

c) Suppose an additional 1 MW were attached to this power system would be the new f_{sys} , P_{G_1} & P_{G_2} ?

$$\boxed{3.5 = P_{G_1} + P_{G_2}} \Rightarrow \boxed{f_{sys} = 59.5}$$

d) what will the system frequency and generation powers be if the governor setting of G_2 is increased by half Hz ?

$$P_{N1} = 61.5 \quad P_{N2} = 61.5$$

$$P_{G1} + P_{G2} = 3.5 \Rightarrow P_{sgs} = 59.57$$

$$P_{G1} = 1.75 \text{ MW}$$

$$P_{G2} = 1.75 \text{ MW}$$

Example

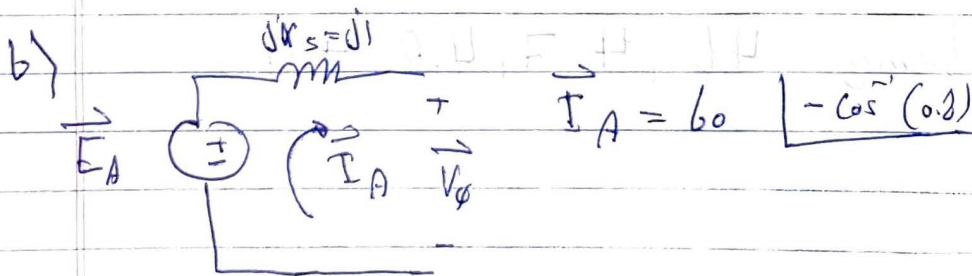
A 480 V, 50 Hz, Y-connected, 6 poles SG has $X_s = 1 \Omega$
 its full load current is 60 A at 0.8 PF lagging friction &
 winding losses = 1.5 kW
 core losses = 1 kW

The field current has been adjusted so that
 $V_T = 480 \text{ V}$ at no load.

- what is the speed of rotation of this generator?
- what is the terminal voltage of the generator at full load?
- what is the efficiency under full load condition?

$$a) \omega_m = \frac{2}{p} \omega_e = \frac{2}{6} (2\pi (50)) \Rightarrow \omega_m = \frac{1000\pi}{30} \text{ rad/sec}$$

$$= 1000 \text{ rpm}$$



$$\vec{E}_A = (jX_s I_A + \vec{V}_\phi) \Rightarrow \sqrt{\frac{1}{3}} 480 \angle \delta = 60 + j1 (60 \angle -\cos^{-1}(0.8))$$

$$\sqrt{\frac{1}{3}} (480) =$$

$$36.87$$

$$j1 (60 \cos(36.87)) + 60$$

$$\sin(36.87)$$

$$= V_{\phi} + b_0 \sin(36.27^\circ) + j b_0 \cos(36.27^\circ)$$

$$\sqrt{\frac{2}{3}} 480 = \sqrt{(V_{\phi} + b_0 \sin(36.27^\circ))^2 + (b_0 \cos(36.27^\circ))^2}$$

$$V_{\phi} = 236.8 \text{ V RMS}$$

$$V_T = \sqrt{3} (236.8) = 410 \text{ V}$$

$$c) P_{out} = \sqrt{3} V_T I_A \text{ PF}$$

$$P_{out} = 34.1 \text{ kW}$$

$$P_{in} = 34.1 + 1 + 1.5 = 36.6 \text{ kW}$$

$$\eta = \frac{34.1}{36.6} = 93.2\%$$

d) Find T_{app} ?

$$T_{app} = \frac{P_{in}}{\omega} = 291 \text{ N}$$

Homework Problems 4.6, 4.7, 4.8, 4.9